



		Number	Algebra		Ratio, Proportion and Rates of Change		Geometry and Measures	Proba	bility and Statistics
KS3 Overview	•	consolidate their numerical and mathematical capability from key stage 2 and extend their understanding of the number system and place value to include decimals, fractions, powers and roots select and use appropriate calculation strategies to solve increasingly complex problems use language and properties precisely to analyse number interpret when the structure of a numerical problem requires additive, multiplicative or proportional reasoning move freely between different numerical representations	<ul> <li>use language and properties precisely to analyse algebra</li> <li>use algebra to generalise the structure of arithmetic, including to formulate mathematical relationships</li> <li>substitute values in expressions, rearrange and simplify expressions, and solve equations</li> <li>develop algebraic and graphical fluency, including understanding linear and simple quadratic functions</li> <li>identify variables and express relations between variables algebraically and graphically</li> <li>make and test conjectures about patterns and relationships; look for proofs or counterexamples</li> <li>move freely between different algebraic representations</li> </ul>	•	their knowledge of ratio and proportion in working with measures and geometry, and in formulating proportional relations algebraically	•	use language and properties precisely to analyse 2-D and 3-D shapes begin to reason deductively in geometry including using geometrical constructions	• exp	e language and operties precisely to alyse probability and atistics olore what can and anot be inferred in atistical and obabilistic settings, at begin to express eir arguments armally.

- understanding of place value and be able to order positive and negative integers and decimals, using =, ≠, <, >, ≤, ≥
- Accurately interpret and compare numbers in standard form
- use concepts of prime numbers, factors, multiples, common factors, common multiples, HCF and LCM and prime factorisation, including product notation and the unique factorisation property with highly developed success
- Accurately use all operations with integers, decimals, proper and improper fractions and mixed numbers using the order of operations alongside, including powers and roots.
- Be able to use exact roots and decimal

- Accurately use and interpret algebraic notation including ab, 3y,  $\frac{x}{y}$ ,  $x^2$ , brackets and coefficients
- substitute numerical values into formulae and expressions, including scientific formulae with highly developed success
- Comprehensively understand and use concepts and vocabulary of expressions, inequalities, terms and factors
- Accurately simplify algebraic expressions by collecting like terms, expanding brackets and factorising
- Rearrange formulae to change the subject accurately
- Accurately model situations or procedures by translating them into algebraic expressions or formulae and by using graphs
- Solve linear equations in one variable with highly developed success
- Work with coordinates in all four quadrants with highly developed success

- change accurately between related standard units and write in the form 1:n and n:1
- use scale factors, scale diagrams and maps with highly developed success
- express one quantity as a fraction of another accurately
- use ratio notation with highly developed success
- Accurately divide a given quantity into two parts in a given part:part or part:whole ratio; express the division of a quantity into two parts as a ratio
- understanding that a multiplicative relationship between two quantities can be expressed as a ratio or a fraction
- relate the language of ratios and the associated calculations to the arithmetic of fractions and to linear functions

- Derive and apply formulae to accurately calculate and solve problems involving perimeter and area of triangles, parallelograms, trapezia and volume of cuboids and other prisms
- Calculate and solve problems with circles and composite shapes with highly developed success
- Draw and measure line segments and angles in geometric figures with highly developed success
- derive and use the standard rule and compass constructions such as perpendicular bisectors, a perpendicular to a given line from/at a given point and angle bisectors accurately
- describe, sketch and draw using conventional terms and notations (points, lines, parallel lines, perpendicular lines, right angles and polygons that are reflectively and rotationally symmetric
- Accurately use standard conventions for labelling sides and angels and know the criteria for congruency of triangles

- Record, describe and analyse the frequency of outcomes of simple probability experiments involving randomness, fairness, equally and unequally likely outcomes, using appropriate language and the 0-1 probability scale with highly developed success
- Accurately enumerate sets and unions/intersections of sets systematically, using tables, grids and Venn diagrams
- Generate theoretical sample spaces for single and combined events with equally likely, mutually exclusive outcomes and use these to calculate theoretical probabilities with highly developed success
- Comprehensively describe, interpret and compare observed distributions of a single variable through:

- approximations with highly developed success
- Work interchangeably with fractions, decimals and percentages
- Comprehensive
   understanding of
   percentages as 'number
   of parts per hundred'
   and work confidently
   with percentages,
   including percentages
   greater than 100%
- Use standard units with different quantities and change between them accurately.
- Round integers and decimals appropriately including significant figures and use this to estimate calculations with highly developed success and calculate possible resulting errors expressed using inequality notation a<x≤b</li>

- recognise, sketch and produce graphs of linear and quadratic functions of one variable using x and y
- Comprehensively interpret mathematical relationships both algebraically and graphically
- calculate and interpret gradients and intercepts of linear equations numerically, graphically and algebraically with highly developed success
- Accurately use linear and quadratic graphs to estimate values of y for given values of x and vice versa and to find approximate solutions of simultaneous equations
- Find approximate solutions to contextual problems from given graphs of a variety of functions including piecewise linear, exponential and reciprocal graphs
- Accurately generate terms of a sequence from term to term or position to term rules

- solve problems involving percentage change with highly developed success
- solve problems involving direct and inverse proportion with highly developed success
- use compound units such as speed, unit pricing and density to solve problems with highly developed success
- Comprehensively understand gradient of a line as a ratio

- derive and illustrate properties of triangles, quadrilaterals, circles and other geometrical figures with appropriate comprehensive language.
- be able to recognise transformations such as translation, reflection rotation and be able to recognise and describe them with highly developed success
- Be able to accurately construct similar shapes using enlargement and describe enlargements
- apply the properties of angles at a point, angles on a straight line and vertically opposite angles with highly developed success
- Comprehensively understand the relationships with angles in parallel lines such as corresponding and alternate angles
- Derive the sum of angles in a triangle and use it to work out the angles in any polygon and derive properties of regular polygons
- Accurately apply angles facts, triangle congruence, similarity and properties of quadrilaterals

- appropriate graphical representation involving discrete, continuous and grouped data; and appropriate measures of central tendency (mean, mode, median) and spread (range, consideration of outliers)
- Accurately construct and interpret appropriate tables, charts, and diagrams, including frequency tables, bar charts, pie charts, and pictograms for categorical data, and vertical line (or bar) charts for ungrouped and grouped numerical data
- Describe comprehensive mathematical relationships between two variables (bivariate data) in observational and experimental contexts and illustrate using scatter graphs.

	<ul> <li>Recognise arithmetic sequences and find the nth term with highly developed success</li> <li>Recognise geometric sequences and appreciate other sequences that arise</li> </ul>		to derive results about angles and sides, including pythagoras' theorem, and use known results to obtain simple proofs  • Be able to use pythagoras' theorem with highly developed success and trigonometric ratios in similar triangles to solve problems involving right-angled triangles	
• Effectively understand place value and be able to order positive and negative integers and decimals, using =, ≠, <, >, ≤, ≥ • interpret and compare numbers in standard form effectively • Confident to use concepts of prime numbers, factors, multiples, common factors, common multiples, HCF and LCM and prime factorisation, including product notation and the unique factorisation property	<ul> <li>Confidently use and interpret algebraic notation including ab, 3y, x/y, x², brackets and coefficients</li> <li>substitute numerical values into formulae and expressions effectively, including scientific formulae</li> <li>Sound understanding and use concepts and vocabulary of expressions, inequalities, terms and factors</li> <li>simplify algebraic expressions by collecting like terms, expanding brackets and factorising confidently</li> <li>Rearrange formulae to change the subject effectively</li> </ul>	<ul> <li>change effectively         between related         standard units and write         in the form 1:n and n:1</li> <li>use scale factors, scale         diagrams and maps with         sound understanding</li> <li>Confidently express one         quantity as a fraction of         another</li> <li>use ratio notation</li> <li>divide a given quantity         into two parts in a given         ratio effectively</li> <li>Sound understanding         that a multiplicative         relationship between two         quantities can be         expressed as a ratio or a         fraction</li> </ul>	<ul> <li>Derive and apply formulae to confidently calculate and solve problems involving perimeter and area of triangles, parallelograms, trapezia and volume of cuboids and other prisms</li> <li>Sound understanding of how to calculate and solve problems with circles and composite shapes</li> <li>Draw and measure line segments and angles in geometric figures</li> <li>derive and use the standard rule and compass constructions such as perpendicular bisectors, a perpendicular to a given line from/at a given point and angle bisectors confidently</li> </ul>	<ul> <li>Confidently record, describe and analyse the frequency of outcomes of simple probability experiments involving randomness, fairness, equally and unequally likely outcomes, using appropriate language and the 0-1 probability scale</li> <li>Confidently enumerate sets and unions/intersections of sets systematically, using tables, grids and Venn diagrams</li> <li>Sound ability to generate theoretical sample spaces for single and combined events</li> </ul>

- Be able to use all operations with integers, decimals, proper and improper fractions and mixed numbers using the order of operations alongside, including powers and roots effectively
- Confidently work interchangeably with fractions, decimals and percentages
- define percentages s 'number of parts per hundred' and work confidently with percentages, including percentages greater than 100%
- Sound understanding of standard units with different quantities and effectively change between them.
- Confidently round integers and decimals appropriately including significant figures and use this to estimate calculations

- Confident in modelling situations or procedures by translating them into algebraic expressions or formulae and by using graphs
- **Confidently** Solve linear equations in one variable
- Work confidently with coordinates in all four quadrants
- Confidently recognise, sketch and produce graphs of linear and quadratic functions of one variable using x and y
- Confidently Interpret mathematical relationships both algebraically and graphically
- Effectively calculate and interpret gradients and intercepts of linear equations numerically, graphically and algebraically
- Effectively use linear and quadratic graphs to estimate values of y for given values of x and vice versa

- relate sound language of ratios and the associated calculations to the arithmetic of fractions and to linear functions
- compare using ratios
- solve problems involving percentage change
- solve problems involving direct proportion
- use compound units such as speed and density to solve problems confidently.

- Effectively describe, sketch and draw using conventional terms and notations (points, lines, parallel lines, perpendicular lines, right angles
- Sound understanding of standard conventions for labelling sides and angels and know the criteria for congruency of triangles
- Confidently derive and illustrate properties of triangles, quadrilaterals, circles and other geometrical figures with appropriate language.
- be able to soundly recognise transformations such as translation, reflection rotation and be able to recognise and describe them
- Be able to confidently construct similar shapes using enlargement and describe enlargements
- apply the properties of angles at a point, angles on a straight line and vertically opposite angles effectively
- Sound understanding of the relationships with angles in parallel lines such as

- with equally likely, mutually exclusive outcomes and use these to calculate theoretical probabilities.
- Effectively describe, interpret and compare observed distributions of a single variable through appropriate graphical representation involving discrete, continuous and grouped data
- Confidently describe, interpret and compare appropriate measures of central tendency (mean, mode, median) and spread (range, consideration of outliers)
- Construct and interpret frequency tables, bar charts, pie charts, pictograms and vertical line (or bar) charts
- Soundly describe simple mathematical relationships between two variables (bivariate data) in observational and experimental

		<ul> <li>generate terms of a sequence from term to term or position to term rules</li> <li>Recognise arithmetic sequences with sound understanding</li> </ul>		corresponding and alternate angles  Confidently derive the sum of angles in a triangle and use it to work out the angles in any polygon and derive properties of regular polygons  Be able to use pythagoras' theorem	contexts and illustrate using scatter graphs.
Foundation (Some/Basic/Limited access)	<ul> <li>understand basic place value and be able to order positive and negative integers and decimals, using =, ≠, &lt;, &gt;, ≤, ≥</li> <li>use basic concepts of prime numbers, factors, multiples, common factors, common multiples, HCF and LCM and prime factorisation</li> <li>Be able to use all basic operations with integers and decimals and apply order of operations to these, including powers and roots</li> <li>Work interchangeably with fractions, decimals and percentages</li> </ul>	<ul> <li>Some use and interpret algebraic notation including ab, 3y, x/y, x², brackets and coefficients</li> <li>Basic understanding to substitute numerical values into formulae and expressions, including scientific formulae</li> <li>Basic understanding and using concepts and vocabulary of expressions, inequalities, terms and factors</li> <li>simplify algebraic expressions by collecting like terms, expanding brackets and factorising at basic level</li> </ul>	<ul> <li>change freely between related basic understanding of standard units</li> <li>use scale factors, scale diagrams and maps with limited access</li> <li>use basic understanding to express one quantity as a fraction of another</li> <li>use ratio notation</li> <li>use basic understanding to divide a given quantity into two parts in a given ratio</li> <li>understand that a multiplicative relationship between two quantities can be expressed as a ratio or a fraction</li> </ul>	<ul> <li>derive and apply basic formulae to calculate and solve problems involving perimeter and area of triangles, parallelograms, trapezia and volume of cuboids</li> <li>show basic understanding in drawing and measuring line segments and angles in geometric figures</li> <li>derive and use the basic standard rule and basic compass constructions such as perpendicular bisectors and angle bisectors</li> <li>use some understanding to describe, sketch and draw using conventional terms and notations (points, lines, parallel lines, perpendicular lines, right angles</li> <li>use standard conventions for labelling sides and angels and</li> </ul>	<ul> <li>Record, describe and analyse the frequency of outcomes of simple probability experiments involving randomness, fairness and equally likely outcomes, using appropriate language and the 0-1 probability scale</li> <li>Understand that the probabilities of all possible outcomes sum to 1</li> <li>Describe, interpret and compare appropriate basic understanding of graphical representations involving discrete, continuous and data</li> </ul>

- Define percentages s 'number of parts per hundred' and work confidently with percentages
- Use standard units with different quantities and change between them using some understanding
- Round integers and decimals appropriately

- Apply limited understanding to rearrange formulae to change the subject
- Solve **some** linear equations in one variable
- Work with coordinates in all four quadrants
- recognise, sketch and produce graphs of linear and quadratic functions of one variable using x and y with limited understanding
- generate terms of a sequence from term to term or position to term rules using basic understanding

- relate the **basic** language of ratios and the associated calculations to the arithmetic of fractions and to linear functions
- solve basic problems involving percentage change
- solve some problems involving direct proportion
- use compound units such as speed and density to solve problems.

- know the criteria for congruency of triangles
- derive and illustrate properties of triangles, quadrilaterals, circles and other geometrical figures with appropriate language.
- be able to recognise transformations such as translation, reflection rotation and be able to recognise and describe them with some understanding
- Be able to construct similar shapes using basic understanding of enlargement and describe enlargements
- apply the properties of angles at a point, angles on a straight line and vertically opposite angles
- Understand the basic relationships with angles in parallel lines such as corresponding and alternate angles
- Derive the sum of angles in a triangle using basic knowledge
- Be able to use basic understanding of pythagoras' theorem with

- Describe, interpret and compare the mean, mode, median and range (considering outliers)
- With some
   understanding construct
   and interpret frequency
   tables, bar charts, pie
   charts, and pictograms
   for categorical data, and
   vertical line (or bar)
   charts for ungrouped
   and grouped numerical
   data
- Describe basic mathematical relationships between two variables using scatter graphs.